$$\lim_{x \to 0} f(x) = \frac{1}{2} \, g'(0) = \frac{1}{2} e^0 = \frac{1}{2}$$