

3. incertitudes:

$$\begin{aligned}a &= (1,1 \pm 0,1) \text{ cm} \\b &= (0,8 \pm 0,1) \text{ cm} \\c &= (5,5 \pm 0,1) \text{ cm} \\\alpha &= (60,2 \pm 0,1)^\circ\end{aligned}$$

Calcul du volume V :

$$\begin{aligned}V &= a \times b \times \sin(\alpha) \times c \\V &= 1,1 \times 0,8 \times 5,5 \times \sin(60,2) \\V &= 4,2 \text{ cm}^3\end{aligned}$$

Calcul de l'incertitude absolue

$$V = f(a; b; c; \alpha)$$

$$\bullet \frac{\partial f}{\partial a} = 0,8 \times 5,5 \times \cos(60,2) = 2,19$$

$$\bullet \frac{\partial f}{\partial b} = 1,1 \times 5,5 \times \cos(60,2) = \cancel{0,44} 3,01$$

$$\bullet \frac{\partial f}{\partial c} = 1,1 \times 0,8 \times \sin(60,2) = 0,44$$

$$\bullet \frac{\partial f}{\partial \alpha} = 1,1 \times 0,8 \times 5,5 = 4,84$$

$$\Delta V = \left| \frac{\partial f}{\partial a} \right| \times \Delta a + \left| \frac{\partial f}{\partial b} \right| \times \Delta b + \left| \frac{\partial f}{\partial c} \right| \times \Delta c + \left| \frac{\partial f}{\partial \alpha} \right| \times \Delta \alpha$$

$$\Delta V = 2,19 \times 0,1 + 3,01 \times 0,1 + 0,44 \times 0,1 + 4,84 \times 0,1$$

$$\Delta V = 1,048$$

$$\text{Donc } V(4,2 \pm 1,048) \text{ cm}^3$$

Calcul de l'incertitude relative $\frac{\Delta V}{V}$

$$\frac{\Delta V}{V} = \frac{1,048}{4,2} = 0,25$$